

Lecture 5: ***Introduction to Modeling***

COSMOS - Making Robots and
Making Robots *Intelligent*



The Model Allows Response Prediction

Given a **starting condition**, and a **model**

(*think - iterated map ~ discrete-time dynamics*)

we can **predict** what our robot will do.

==> Prediction reliable in short term.



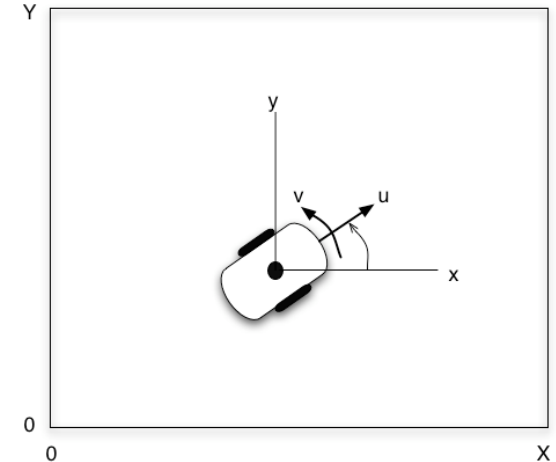
“Bobs” response:
$$v_{k+1} = v_k + \frac{\Delta}{m} [-(b + K)v_k + K v_{des} + u_{hill}(t_k)]$$

Robobrian Model:

$$x_{k+1} = x_k + \Delta u_k \cos(\theta_k)$$

$$y_{k+1} = y_k + \Delta u_k \sin(\theta_k)$$

$$\theta_{k+1} = \theta_k + \Delta v_k$$



Stability: Design control (u, v) so (x, y, θ) achieve desired values.

Next Step - Choice of Feedback Control

Model of “Bob”:

$$mv_{k+1} = mv_k + \Delta[-bv_k + u_{eng} + u_{hill}]$$

Control:

$$u_{eng} = K(v_{des} - v_k), \quad K > 0$$



Steady-state (when $v_k = v_{ss}$, $k = 0, 1, 2, \dots$):

$$\implies v_{ss} = \underbrace{\frac{K}{b+K}}_{\text{Goes to 1 as } K \rightarrow \infty} v_{des} + \underbrace{\frac{1}{b+K}}_{\text{Goes to 0 as } K \rightarrow \infty} u_{hill}$$

Goes to 1 as $K \rightarrow \infty$

Goes to 0 as $K \rightarrow \infty$

Why this choice for control? How do we choose (u, v) for Robobrain? \implies Key form is feedback error signal: $(x, y, \theta) - (x_{des}, y_{des}, \theta_{des})$

Objective

- Understanding of Modeling using Iterated Maps
- Using Matlab for Prediction using Model. Predator-Prey System Example.
- Robobrain Model and Control Objectives.