MAE140 Linear Circuits (for non-electrical engs)

Topics covered

Circuit analysis techniques

Kirchoff's Laws-KVL, KCL

Nodal and Mesh Analysis

Thévenin and Norton Equivalent Circuits

Resistive circuits, RLC circuits

Steady-state and dynamic responses

Impulse and step responsesLaplace transformsSinusoidal steady-state response

Circuit design techniques

Active circuit elements – dependent sources and operational amplifiers Feedback basics

Signal filtering – if we get time

What do I expect you to know?

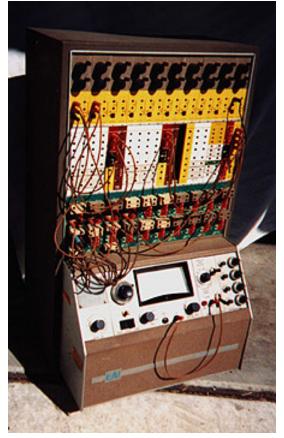
Prerequisites

Mathematics 21D or 20D (some are doing this concurrently) Solution of sets of linear equations Ax=b equations for vector x given matrix A and vector b Solution of constant coefficient linear ordinary differential equations Laplace transform introduction Initial conditions and forced response Complex analysis Numbers, arithmetic, magnitudes and phases, poles, zeros Physics 2B Behavior of circuit elements: R, L and C Underlying physical principles

Why should you be excited about MAE140?

Linear circuits are exceptionally well described by simple and powerful mathematics

The quality of concordance between measured physical behavior and mathematical description is amazing



This is an analog computer from around 1963 It was used to solve nonlinear ODEs via analog circuitry

It contained: about 20 integrators based on valves or transistors, some nonlinear function blocks using diodes, comparators This was the state of the art for much physical system simulation

It relies on ideas underpinning MAE140 The tools of MAE140 are immediately useful in design

Why should you still be excited about MAE140?

The *front and back ends* of your digital cell phone are comprised of analog circuits

This is pretty much true of all *digital* technology Why does the stagecoach wheel appear to rotate backwards? Aliasing

A high frequency masquerading as a low frequency Anti-aliasing filters MUST be used in all sampled data systems

After MAE140 you will be able to start designing such anti-aliasing filters The real thing!



Why should you still be excited about MAE140?

You will learn how these knobs and plugs work:



We will not have time to cover this one:



Why should you still be excited about MAE140?

Google" Custom S

theguardian

News US World Sports Comment Culture Business Money Environment Science

News World news Nuclear weapons

Ed Pilkington in New York

US nearly detonated atomic bomb over North Carolina – secret document

Exclusive: Journalist uses Freedom of Information Act to disclose 1961 accident in which one switch averted catastrophe



Follow The Guardian, Friday 20 September 2013 12.03 EDT



The bomb that nearly exploded over North Carolina was 260 times more powerful than the device which devasted Hiroshima in 1945. Photo: Three Lions/Getty Images

A secret document, published in declassified form for the first time by the Guardian today, reveals that the US Air Force came dramatically close to detonating an atom bomb over North Carolina that would have been 260 times more powerful than the device that devastated Hiroshima.

The document, obtained by the investigative journalist Eric Schlosser under the Freedom of Information Act, gives the first conclusive evidence that the US was narrowly spared a disaster of monumental proportions when two Mark 39 hydrogen bombs were accidentally dropped over Caldebase Next Overline 22 Jacoust 4004. The best follower the follower the

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Eric Schlosser: 'The people who are most anti-nuclear are the ones who know most about it' The US author talks about his six-year allout immersion in the terrifying and surreal world of nuclear weapons for his latest book, Command and Control "The bombs fell to earth after a B-52 bomber broke up in mid-air, and one of the devices behaved precisely as a nuclear weapon was designed to behave in warfare: its parachute opened, its trigger mechanisms engaged, and only **one lowvoltage switch** prevented untold carnage."

"... a senior engineer in the Sandia national laboratories responsible for the mechanical safety of nuclear weapons concludes that 'one simple, dynamo-technology, **low voltage switch** stood between the United States and a major catastrophe.""



Circuit variables (T&R Chap 1)

Charge and Energy

-1 coulomb (C) = 6.25×10^{18} electrons' charge $i = \frac{dq}{dq}$ 1 ampere (A) = 1 coulomb/second Current is a measure of charge passing Direction of flow is of positive charge This is important for understanding some devices Voltage/potential difference/electromotive force/tension Voltage measures the energy gained by a charge 1 joule(J)/coulomb = 1 volt(V)da Voltage is measured between two points (potential difference) This is akin to gravitational potential and fluid flow or temperature and heat flow

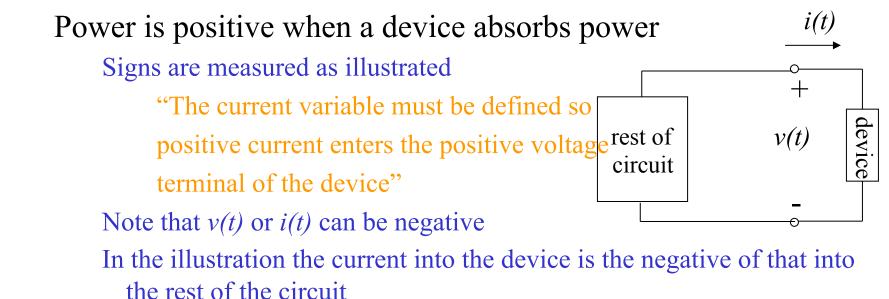
Circuit variables (contd)

Power is the rate of energy change per unit time $p = \frac{dw}{dt}$ watts (W)

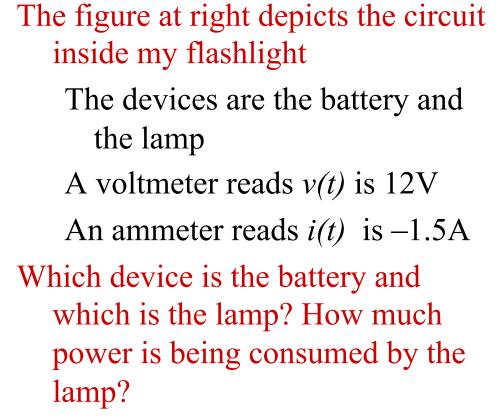
Note the chain rule
$$p = \left(\frac{dw}{dq}\right) \left(\frac{dq}{dt}\right) = vi$$

The instantaneous electrical power associated with a voltage and a current flow is given by the product $v \times i$

Passive sign convention



An example

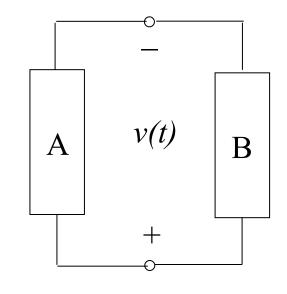


Using the passive sign convention

The power absorbed by device A is 12×1.5 W = -18 W

A is the battery and B is the lamp, which consumes 18W





Circuit variables (contd)

Ground

Because all voltages are measured between two points, there is no absolute voltage - it is a potential

In circuits we often refer all voltages of points as being relative to a fixed point or *ground* voltage This is depicted win the complete $\begin{pmatrix} v_A(t) & v_B(t) & v_C(t) \\ + \circ & + \circ & + \circ \\ A & B & C \end{pmatrix}$

This is depicted via the _____ symbol

The terms v_A etc mean the voltage at A relative to G

This is like referring heights relative to sea level

Gravity is also a potential

Check out the elevator buttons in the Math & App Phys Building!

_ ° G

Circuit variables (contd)

A *circuit* is a collection of interconnected electrical devices

For us:

All electromagnetic interactions in the circuit take place within the devices (This is a *lumped-parameter* circuit) The circuit devices are connected together by wires which are ideal They have the same voltage at both ends instantaneously They propagate current without loss instantaneously They may be stretched arbitrarily without changing properties All circuit devices have at least two terminals and are assumed not to accumulate charge – current in equals current out A *node* is the junction of terminals of two or more devices A *loop* is a closed path formed by tracing through an ordered sequence of nodes without passing through any node more than once

Circuit variables

The important physical circuit variables are currents into and voltages across circuit elements and their associated power consumption or production.

- *Circuit analysis* consists of solving for the circuit variables in a given circuit
- *Circuit design* or *synthesis* consists of constructing a circuit whose circuit variables exhibit a specified behavior

The *topology* of a circuit is the key structure It can be stretched and wrapped around without changing circuit variables

Nodes can be stretched and shrunk to cover many terminals

Circuit Topology

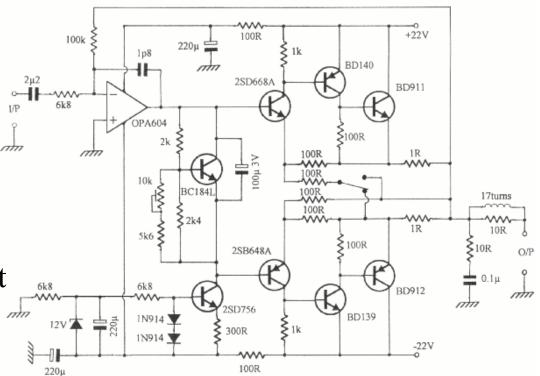
This is the circuit diagram of an audio amplifier

It shows the relationship between parts but not their actual physical location

- The ground/earth is likely the ______ chassis or case
- The output transistors BD912 and BD911 will need to be attached to an external heat sink

The op-amp OPA604 will be board mounted

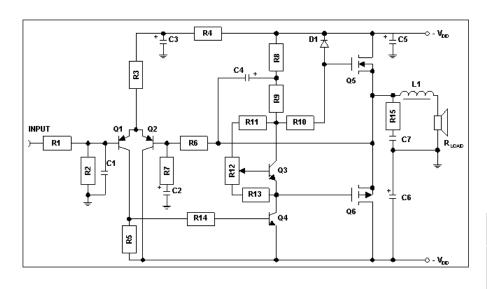
The volume control needs to be accessible



Circuit Topology – high power amplifier with complementary HEXFETS

Circuit Diagram

Circuit Board Layout



HEXFET – power MOSFET from International Rectifier

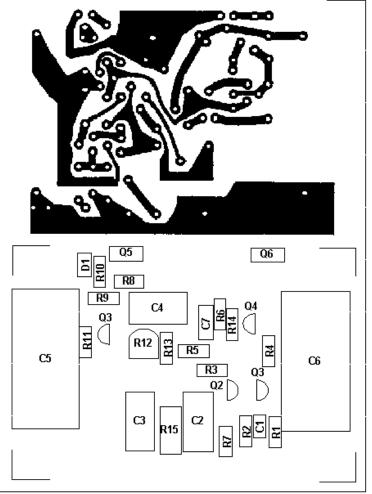


Figure 2. Amplifier Printed Circuit Board Layout

MAE140 Linear Circuits

Basic Circuit Analysis (T&R Chap 2)

Kirchoff's Current Law (KCL)

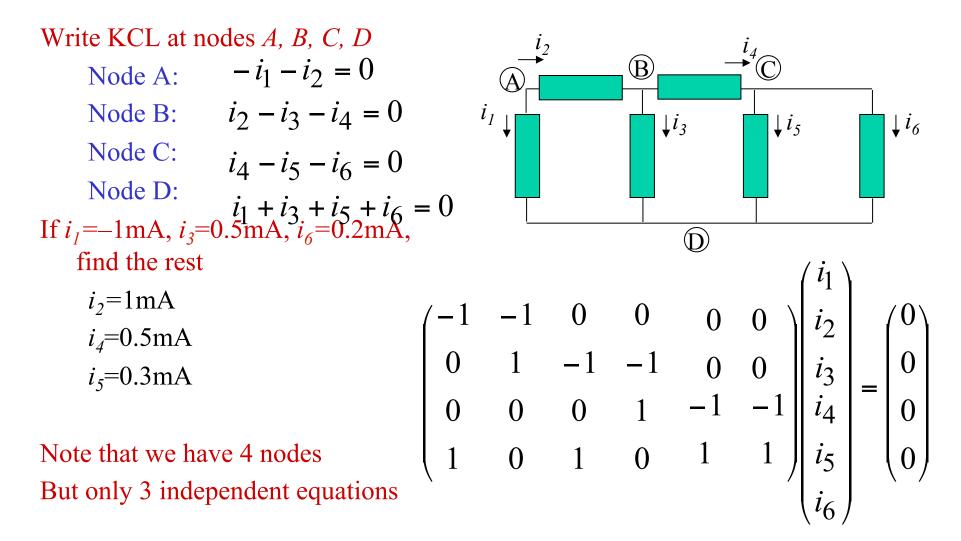
The algebraic sum of currents entering a node is zero at every instant

This is a restatement of the principle of conservation of charge Alternatively, but not so nice,

The sum of currents entering a node is equal to the sum of currents leaving a node at every instant

KCL provides linear constraints between the currents in a circuit In a circuit containing a total of N nodes there are only N-1 independent KCL connection equations

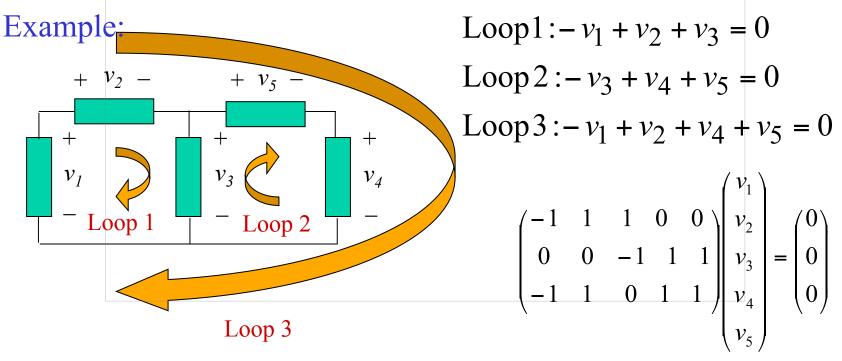
T&R, 5th ed, Exercise 2-1 p 22



Kirchoff's Voltage Law (KVL)

The algebraic sum of voltages around a loop is zero at every instant the image cannot be displayed. Your computer may not have enough memory to open the image, or the image may have been corrupted. Restart your computer, and then open the file again. If the red x still appears, you may have to delete the image and the instant it again.

This is really a restatement of voltage as a potential, effectively a statement of the principle of conservation of energy



Circuit Analysis

- One way to consider the analysis of a circuit (i.e. the computation of the currents in and voltage across the circuit elements) is through the specification of constraints on these variables
 - KCL and KVL provide one set of constraints on circuit variables reflecting connection topology
 - The *i-v* properties of the devices themselves provide further constraints

N nodes and E circuit elements

N-1 independent KCL relations

E-N+1 independent KVL relations (number of independent loops)

E independent *i-v* characteristics

2E circuit variables

If we keep to linear devices then we have linear circuit analysis 2E Linear algebraic equations for 2E variables

Linear Circuit Elements

Linearity in *v-i* relations

Doubling v doubles i and vice versa $i = \alpha v$

Straight lines in *i-v* plane

Note that $i = \alpha v + \beta$ describes an *affine* relation

Resistor

v = Ri or i = Gv Ohm's Law

R resistance in ohms (Ω), *G* conductance in siemens (S) Power $P=i^2R=v^2/R=v^2G$

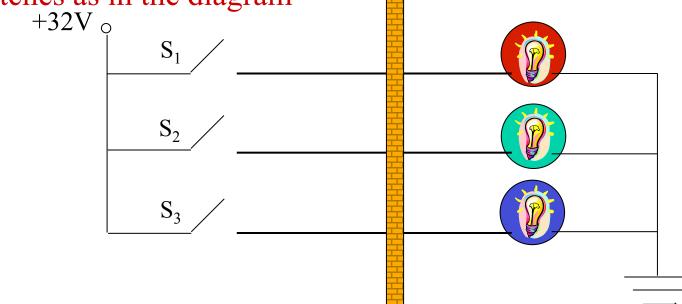
A resistor always absorbs power -i-v line has positive slope This is an instantaneous linear element

We will look at circuit elements with memory like *C* and *L* later in the course

V

Time out puzzle

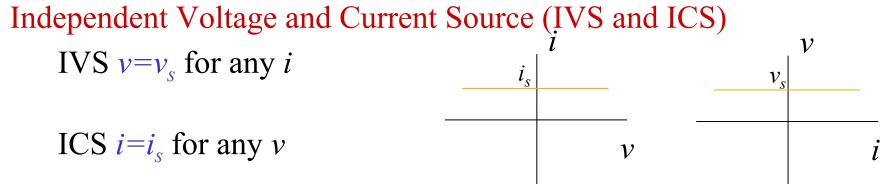
We have three lamps – red, green and blue – connected to three switches as in the diagram



The lamps are outside the switch room and we are alone What single test can we perform by playing with the switches to determine which switch is connected to which light?

I know of two solutions, one of physicists, one of engineers

Linear Circuit Elements (contd)



Affine elements rather than linear, but we admit them

Most sources of electrical energy (batteries, generators, power systems) are modeled as voltage sources. Examples of current sources include diode and transistor current sources

Open circuit and short circuit – variants of ICS and IVS resp.

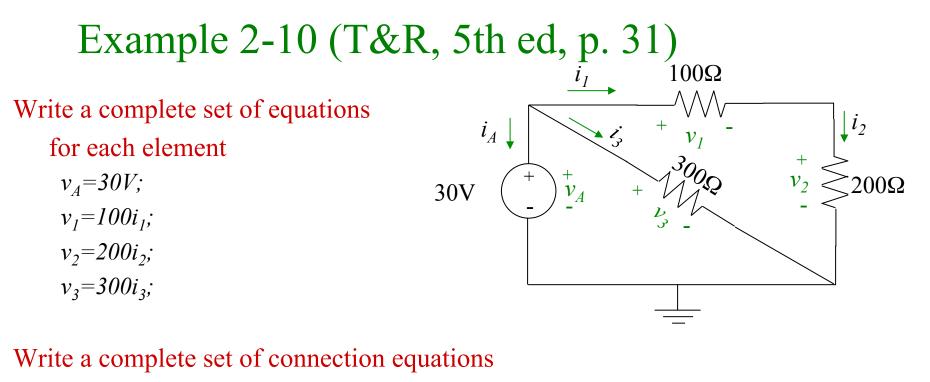
Open circuit $i=0$ for any v	Same as $R = \infty$
Short circuit $v=0$ for any <i>i</i>	Same as $R=0$

These are truly linear since the curves pass through (0,0)

Switches – either o.c. or s.c.

Write a complete set of connection equations

Solve these equations for all currents and voltages



 $-i_{A}-i_{I}-i_{3}=0;$ $i_{I}-i_{2}=0;$ $-30+v_{3}=0;$ $v_{I}+v_{2}-v_{3}=0;$

Solve these equations for all currents and voltages

 $v_A = 30V;$ $v_1 = 10V;$ $v_2 = 20V;$ $v_3 = 30V;$ $i_A = -200mA;$ $i_1 = i_2 = i_3 = 100mA;$

All you ever wanted to know about resistors ...

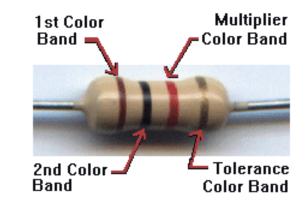
Resistors are color coded to indicate their value

Black	Brown	Red	Orange	Yellow	Green	Blue	Violet	Grey	White
0	1	2	3	4	5	6	7	8	9

and tolerance

5%	10%	20%
Gold	Silver	Empty

This is a $1K\Omega$ resistor with 5% tolerance



Resistors come at standard values (e.g., at 10% tolerance)

1	1.2	1.5	1.8	2.2	2.7	3.3	3.9	4.7	5.6	6.8	8.2	Nominal
.9	1.08	1.35	1.62	1.98	2.43	2.97	3.51	4.23	5.04	6.12	7.38	Lower
1.1	1.32	1.65	1.98	2.42	2.97	3.63	4.29	5.17	6.16	7.48	9.02	Upper

Even more than you ever wanted to know about resistors ...

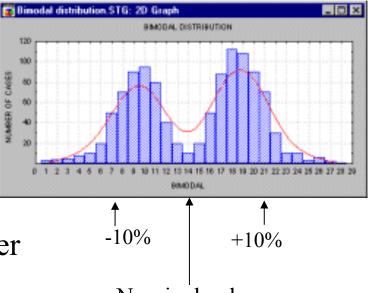
The distribution of resistances Why should this be so?

How can we get a 258.3Ω resistor?

Keep testing the ones in the box

A really finely tunable potentiometer

(variable resistor) – a *trimpot*



Nominal value

A coarsely tunable potentiometer in parallel with a lower *R* Make one from high precision components

Another important characteristic of *R* is the power rating Why?