## MAE40 - Linear Circuits - Fall 23 - Section A00 <br> Midterm \#1, October 24

## Instructions

(i) The exam is open book. You may use your class notes and textbook.
(ii) The exam has 3 questions for a total of 23 points and 2 bonus points.
(iii) You have from 11:00am to $12: 20 \mathrm{pm}$ to do the exam, but it should require less time for you to complete it.
(iv) You can use a calculator with no communication capabilities.
(v) In your responses, clearly articulate your reasoning, and properly justify the steps.
(vi) Important: start each part below on a separate page, use only one side, and write your name \& PID at the top of each page.


Figure 1: Circuit for questions 1 and 2.

Good luck!

## 1. Circuit analysis

Part I: [6 points] Formulate node-voltage equations for the circuit in Figure 1. Use the node labels provided in the figure. Clearly indicate the final equations and circuit variable unknowns. The final equations in matrix form must depend only on unknown node-voltages. Do not modify the circuit or the labels. No need to solve any equations!
Part II: [2 points] Provide expressions for the voltage $v_{x}$ and the current $i_{x}$ in terms of node voltages.
Part III: [2 points] A technician replaced the resistor $R_{4}$ by a short circuit. How did that affect the values of $v_{x}$ and $i_{x}$ ?
2. Linearity and equivalent circuits

For this question, assume $v_{S}=10 \mathrm{~V}, i_{S}=-1 A, R_{1}=R_{2}=R_{3}=R_{5}=5 \Omega$.
Part I: [3 points] Turn off all the sources in the circuit of Figure 1 and find the equivalent resistance as seen from terminals (A) and (B).
Part II: [3 points] Turn off the current source and compute the open-circuit voltage as seen from terminals (A) and (B) using association of resistors, equivalent sources, and voltage division.
Part III: [3 points] Turn off the voltage source and compute the open-circuit voltage as seen from terminals (A) and (B) using association of resistors, equivalent sources, and current division.
Part IV: [1 point] Use superposition and your answers to Parts I-III to determine the Thévenin equivalent of the circuit as seen from terminals (A) and (B).
Part V: [Extra 2 points] If we connect a $12 \Omega$ resistor to terminals (A) and (B), what is the minimum power rating that this resistor should have?
3. Real-world power supply [3 points]

For the real-world power supply in Figure 2 with an output specification of 24 VDC, 1A, indicate in the table below the voltage output from the power supply for the values of $R$.

| $R$ | voltage output from power supply |
| :--- | :--- |
| $100 \Omega$ |  |
| $10 \Omega$ |  |
| $1 \Omega$ |  |



Figure 2: Circuit for question 3.

